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1 **Optimization of sampling design for soil total organic carbon assessment in the precision**  
2 **agriculture framework: Impact of different variogram models and potentiality of ground**  
3 **penetrating radar (GPR) covariate information**

4  
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15  
16  
17 **Abstract**

18 Assessing soil organic carbon (SOC) at the field scale is crucial for efficient environmental and  
19 agronomic management, especially within the precision agriculture framework. This enables the  
20 implementation of crop and soil management strategies to enhance soil quality, increase carbon  
21 sequestration, and improve crop yields. However, the process of sampling and assessing SOC is  
22 resource-intensive, demanding both in time and labour. This aspect is particularly relevant also in  
23 agronomic research, where the need to assess the spatial correlation of the investigated variables  
24 requires the collection of large datasets with georeferenced data and often measurements need to be  
25 repeated over time as for long-term field experiment - LTE. Methods for minimizing information loss  
26 while reducing the sampling scheme, such as spatial simulated annealing (SSA), are particularly  
27 valuable in the scope of SOC assessment, especially when faced with budget and time/labour  
28 constraints. Within the structure of the SSA method, two critical components can be identified: i) the  
29 inclusion of highly informative covariates for the primary variable (SOC); ii) the selection of the most  
30 appropriate variogram model for spatial variability assessment. Covariates strongly correlated with

31 SOC, such as those obtained from ground penetrating radar (GPR) that can be collected at a higher  
32 spatial density compared to SOC data, along with a well-performing model, can significantly enhance  
33 the efficiency of the sampling scheme reduction process. We conducted a study using data from an  
34 agronomic field experiment, which included 71 georeferenced sampling locations and, through an  
35 iterative downsizing process utilizing SSA, we progressively reduced the number of sampling points  
36 by removing 10, 15, and 20 observations. The sampling scheme was refined according to two distinct  
37 variogram models: the spherical and Gaussian-Matérn models, both for the primary variable (SOC)  
38 and the covariate GPR variable. This process allowed us to identify the optimal variogram model,  
39 which has a key role in maximizing the reduction of redundant points while preserving those with  
40 valuable information, and to assess the role of the covariate variable both in improving the  
41 optimization of the sampling scheme for SOC and in replacing the primary variable to optimize the  
42 sampling scheme. Finally, to assess the impact of sampling scheme reduction, a validation process  
43 was performed by estimating the dropped points by means of the remaining points using ordinary  
44 kriging and regression kriging and analysing the accuracy of such estimation. Our analysis  
45 demonstrated that it was possible to reduce the original sampling scheme by approximately 20%  
46 equivalent to eliminating 15 sampling points out of 71 without compromising its predictive capability.

47

48 **Keywords:** Ground Penetrating Radar, Precision agriculture, reduction of sampling scheme,  
49 regression kriging, soil organic carbon, spatial simulated annealing, variogram model.

50

## 51 **1. Introduction**

### 52 1.1 *The sampling issue*

53 Evaluating soil properties, particularly organic carbon content, is crucial for both environmental  
54 preservation and effective agricultural management. Understanding the spatial distribution of soil  
55 total organic carbon (SOC) is essential for modelling spatio-temporal dynamics and assessing the  
56 impact of agricultural practices on soil fertility and carbon sequestration (Sherpa et al., 2016; Zhao et

57 al., 2016; De Benedetto et al., 2022). In addition, the assessment of the field-scale spatial variability  
58 of soil organic carbon (SOC) is critical in precision agriculture applications. Precision agriculture is  
59 an environmental-aware approach that supports farmers in optimizing field activities and agronomic  
60 techniques, including soil management, irrigation, and fertilization, by offering a range of innovative  
61 technological tools and applying advanced data analysis methods (Abo-Habaga et al., 2024; Colovic  
62 et al., 2024; Mzid et al., 2023; Zaman, 2023). The primary goal of precision agriculture is to enhance  
63 crop production and resource use efficiency through site-specific practices, demanding a precise  
64 assessment of spatial variations of key variables such as soil organic carbon or soil water content at  
65 fine resolutions. This information aids farmers in identifying homogeneous zones for tailored  
66 agronomic input application (Popolizio et al., 2022a-b; Zaman, 2023).

67 The assessment of the spatial structure of the investigated variables is also an important objective of  
68 agronomic research in order to adopt appropriate statistical models for data analysis. This requires  
69 the collection of large datasets with georeferenced data (Lawrence et al., 2020; Popolizio et al.,  
70 2022a); in addition, often measurements need to be repeated over time as in the case of long-term  
71 field experiments -LTEs. However, obtaining accurate soil and crop property samples can be  
72 challenging and expensive. Therefore, optimizing sampling strategies is essential to provide precise  
73 information at minimal costs. Selecting optimal sampling approaches and data analysis methods is  
74 critical for addressing fine-scale variability and understanding spatial dependencies between  
75 observations and residuals, preventing misleading conclusions about soil property estimations  
76 (Littell, 2006). The process of predicting soil variables typically begins with designing an appropriate  
77 sampling scheme to capture soil heterogeneity effectively (Stein and Ettema, 2003; Warrick et al.,  
78 2002; Jalilian et al., 2024). Common sampling methods include grid-based, simple random, and  
79 stratified random schemes. Grid-based sampling is prevalent at the plot scale, but it can become cost-  
80 prohibitive when applied over large areas (Atkinson and Lloyd, 2007). Optimizing the sampling  
81 design can reduce the number of sampling points with minimal accuracy loss. Critical considerations  
82 in sampling design optimization involve choosing between deterministic (e.g., inverse distance

83 weighted) and stochastic (e.g., kriging) approaches and selecting the appropriate objective or cost  
84 function. When the stochastic approach is preferred, optimizing spatial sampling includes selecting  
85 the optimal model for spatial dependence, typically represented by a variogram model when using  
86 ordinary kriging variance as the objective function.

87

### 88 *1.2 GPR as a source of valuable covariate information and sample redundancy discarding*

89 Another important aspect is the incorporation of covariate information, which can help explain  
90 variability in soil parameters (Tarr et al., 2005). Utilizing covariate variables, such as data from  
91 geophysical sensors, can mitigate the limitations imposed by low sampling density and enhance the  
92 accuracy of soil organic carbon (SOC) estimation.

93 Among these geophysical-based methods, in particular, Ground Penetrating Radar (GPR) has gained  
94 attention for its applications in agriculture and in soil studies to assess various soil properties and their  
95 spatial and temporal variability (Pathirana et al., 2023). Compared to traditional methods, the non-  
96 destructive nature of GPR offers several advantages in agricultural landscape applications, such as  
97 making repeated measurements and providing more extensive spatial coverage with geo-referenced  
98 data. GPR is particularly attractive due to its high resolution and the ability to provide three-  
99 dimensional (3D) information (Liu et al., 2019). The main limits of this technique are the difficulty  
100 of real-time data processing and interpretation. In fact, GPR does not directly measure soil properties  
101 (Pathirana et al., 2023), but its 3D data can be correlated with soil attributes. Incorporating GPR data  
102 as covariates into models like regression kriging and multivariate adaptive regression splines has  
103 proven effective for spatially predicting SOC at the field scale (De Benedetto et al., 2022).

104 In order to reduce sample redundancy, a predictive model is needed. When a stochastic approach is  
105 preferred, the model is composed by: i) the trend component and ii) the stochastic component. The  
106 first component is arranged as a linear model with SOC as response, while the second component is  
107 arranged through the assessment of the variogram model representing the spatial variability of SOC  
108 observations. Since the finding of the best variogram assessment is crucial to maximize the predictive

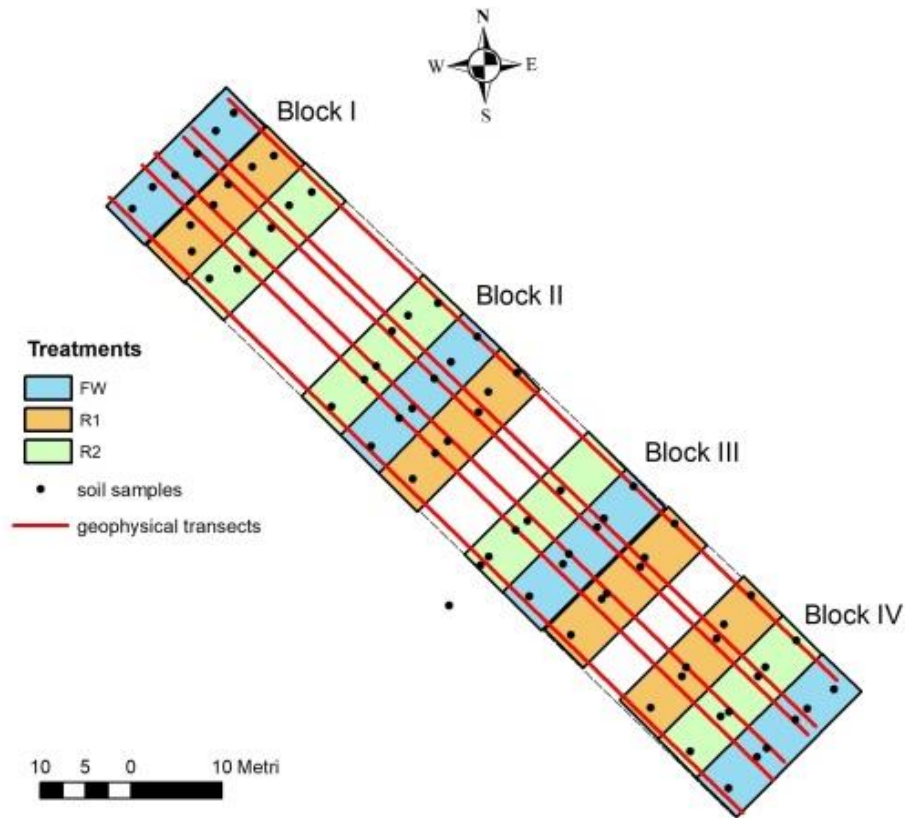
109 capability of the interpolation model, different data-driven approaches are available, such as  
110 Weighted Least Squares (WLS) approach and Restricted Maximum Likelihood (REML).  
111 Once defined the model to predict SOC, the next step is to proceed at reducing the complete sample  
112 design by discarding an increasing number of sampling points. This task can be carried out by means  
113 of Spatial Simulated Annealing (SSA), a largely recognized optimization method. SSA is a heuristic  
114 method based on Markov chain properties, designed to increase the probability of converging towards  
115 the global optimum (Metropolis et al. 1953). SSA checks the predictive capability of any generated  
116 sub-sample by computing the average kriging variance of an estimation grid superimposed over the  
117 study area. The sub-set that achieves the minimum average kriging variance is selected as the best  
118 sub-sample. The R function "spsann" has been run to apply SSA (Samuel-Rosa, 2017).  
119 In this study, our primary goal was to reduce an initially oversized sampling plan for soil total organic  
120 carbon assessment. It is a common practice to initially oversample an area and subsequently optimize  
121 the sampling scheme, for instance in the case of multi-temporal sampling experimental designs  
122 (Popolizio et al., 2022b). Moreover, the study pursued two additional goals: (i) the comparison of two  
123 variogram models in order to select the one with the best capability in reducing SOC sampling  
124 scheme; and (ii) the potential use of GPR information both as covariate variable and in the place of  
125 the primary variable (SOC) within the optimization process. The study was carried out within an  
126 agronomic field experiment where the effect of different irrigation and fertilization management on  
127 soil properties was evaluated. This specific case study was chosen considered the importance of the  
128 assessment of spatial correlation in agronomic research both for adopting appropriate statistical data  
129 analysis approaches and for supporting farmers in delineating management zones and fostering the  
130 application of precision agriculture strategies.

131

## 132 **2. Materials and Methods**

### 133 *2.1. Study area and data collection*

134 Soil data derived from a field experiment (96 m x 20 m) carried out in Southern Italy (40° 50' N, 17°  
135 25' E 26 m above sea level) where the effect of the irrigation and fertilization management on olive  
136 tree were compared. The following treatments were applied: irrigation with fresh water and full  
137 fertilization supply (FW); irrigation with treated municipal wastewater (TWW) and full fertilization  
138 supply (R1); irrigation with TWW and fertilizer supply reduced by the amount provided by TWW  
139 (R2), (De Benedetto et al., 2022). The fertilizer rates corresponding to the full fertilization regime  
140 (FW, R1) were computed considering soil nutrient availability, plant uptakes and target yield and  
141 were equal to: 100 kg ha<sup>-1</sup> of N, 60 kg ha<sup>-1</sup> of P<sub>2</sub>O<sub>5</sub> and 80 kg ha<sup>-1</sup> of K<sub>2</sub>O in 2015 and 110 kg ha<sup>-1</sup> of  
142 N, 60 kg ha<sup>-1</sup> of P<sub>2</sub>O<sub>5</sub> and 85 kg ha<sup>-1</sup> of K<sub>2</sub>O in 2016. In both years, the treated wastewaters contributed  
143 with about 20%, 2% and 70% of the olive fertilizer requirements for N, P<sub>2</sub>O<sub>5</sub> and K<sub>2</sub>O, respectively;  
144 the fertilizer rates of treatment R2 were therefore reduced accordingly. Treatments were arranged in  
145 a randomized complete block design (RCBD) with four replicates (Fig. 1). Soil samples with absolute  
146 coordinates were collected on a regular grid (April 2017) on six locations (sub-replicates, SR) per  
147 plot at a 0-0.20 m depth for a total of 72 observations (3 Treatments x 4 Replicates x 6 SR). For the  
148 data analysis, 71 observations were considered since one was falling outside the sampling grid as  
149 shown in Figure 1. Total organic carbon (SOC) was quantified on air-dried and sieved samples  
150 through dry combustion. Further details about the experimental trial are reported in De Benedetto et  
151 al. (2022).



152

153 *Fig. 1. The field experiment with the soil sampling locations (black dots) and Ground Penetrating*  
 154 *Radar (GPR) acquisitions along transects (red lines). The treatments were: irrigation with fresh*  
 155 *water and full fertilization supply (FW, blue colour), irrigation with treated municipal wastewater*  
 156 *(TWW) and full fertilization supply (R1, orange colour) and irrigation with TWW and fertilizer supply*  
 157 *reduced by the amount provided by TWW (R2, green colour).*

158 A geophysical survey was carried out a GPR sensor (connected to a DGPS) along 6 parallel transects  
 159 by sliding the sensors on the surface (Fig. 1).

160 GPR data used in this study were collected with the common offset reflection method, using a  
 161 monostatic system with two central frequencies of 600 and 1600 MHz (IDS Ing-manufactured, RIS  
 162 2k-MF Multifrequency Array Radar-System). The GPR worked with a time window of 60 ns and a  
 163 sampling interval of 0.05 ns; successive traces were collected every 0.024 m. The successive results  
 164 will be focused on frequency of 600MHz because the maps were less noisy compared with the ones  
 165 of the 1600 MHz antenna, because of their spatial resolution. The GPR produces a short pulse of high

166 frequency (10–1000 MHz) electromagnetic energy which propagates through the sub-surface  
167 materials. The propagation of the radar signal depends on the electrical properties of the soil and  
168 variations in the electrical properties of soils are usually associated with changes in volumetric water  
169 content, porosity, texture, with regard to clay types and clay mineralogy, CEC and dissolved ions in  
170 the soil water present in soil pores (McNeill, 1980). The theoretical aspects of radar components and  
171 their working principles can be found in detail in Davis and Annan (1989).

172

### 173 *2.2.Pre-processing of GPR data*

174 Processing the raw data consisted in extracting quantifiable variables, such as attenuation, and to  
175 display GPR data in horizontal maps at a specified time (or depth), called amplitude maps or time  
176 slices. The pre-processing of GPR signal amplitude data included the application of a set of filters  
177 (De Benedetto et al., 2015) and extracting quantifiable variables. Detailed descriptions of the above  
178 procedures can be found in the historical publications by Reynolds (1997) and Cassidy (2009).

179 The enveloped amplitude maps (time slices) were built averaging the amplitude (or the square  
180 amplitude) of the radar signal, expressed in digital number (DN), within overlapping time windows  
181 of width  $\Delta t$  equal to the order of the dominant period (2 ns). The total time interval was of 20 ns  
182 because this time was comparable with the depth of soil (at 0–0.30 m depth). The time slices were  
183 then transformed in depth slices using the velocity of the radar waves determined through the analysis  
184 of hyperbolae (Daniels, 2004).

185

### 186 *2.3.Mapping data using Geostatistics*

187 SOC map was estimated from 71 data points by ordinary kriging (OK) method (Matheron, 1963) on  
188  $0.5 \times 0.5$ -m grid. The experimental variograms were calculated and fitted using a linear model of  
189 coregionalization (LMC) for GPR data. The fitting parameters, tested by using cross-validation and  
190 calculating mean error (ME) and mean squared standardized error (MSSE) within a typical used

191 tolerance of  $1 \pm 3\sqrt{2/N}$  (where  $N$  is the number of observations), were used to interpolate the data  
192 on the same grid using ordinary cokriging (CK) (Goovaerts, 1997).

193 All geostatistical analyses were performed with ISATIS software (Geovariances, 2015) and with the  
194 following R libraries {automap, spsann}.

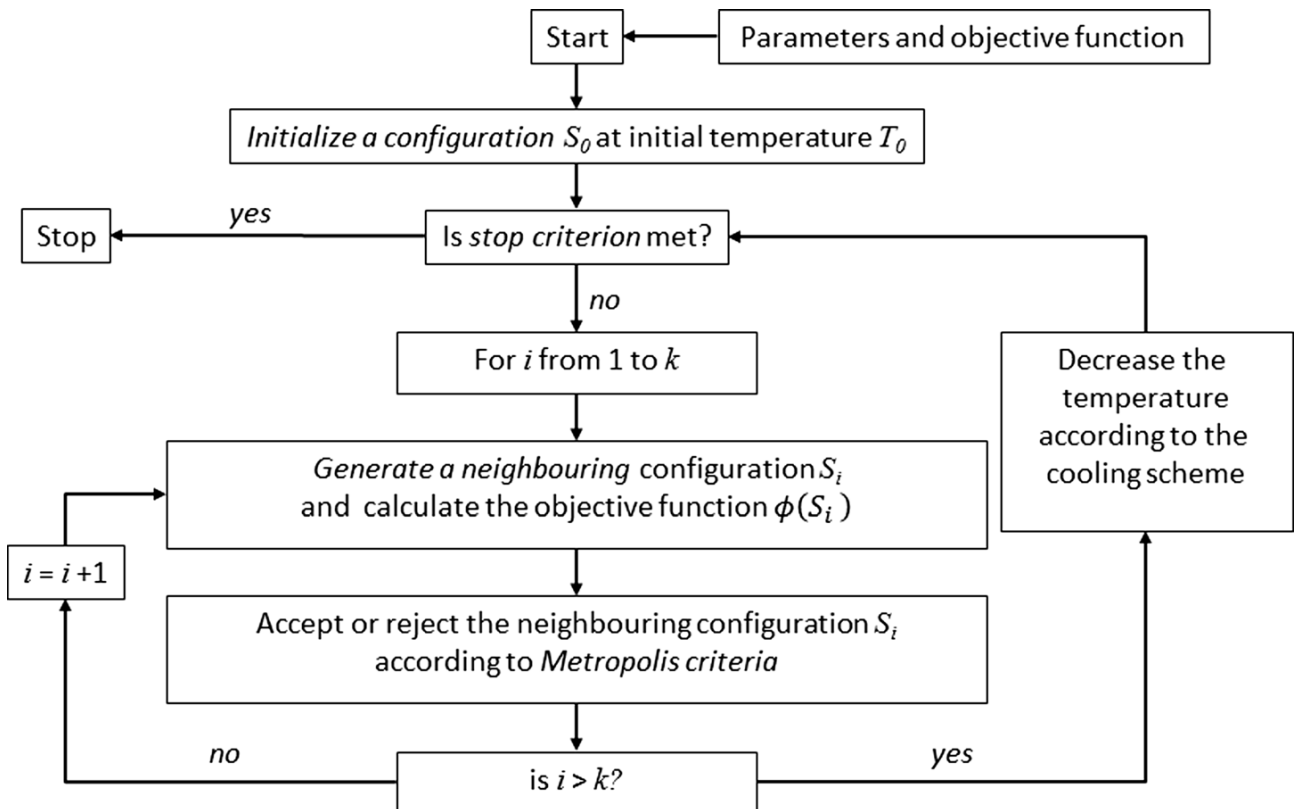
195

#### 196 *2.4. Spatial simulated annealing (SSA)*

197 The Spatial Simulated Annealing (SSA) is an optimization technique designed to efficiently extract  
198 a subset of samples from a larger sampling scheme among those contained in a vast solution space.  
199 Its objective is to minimize a specific objective function while taking advantage from the spatial auto-  
200 correlation of the sampled variable. The theory underlying Spatial Simulated Annealing (SSA) draws  
201 inspiration from the organizational dynamics of a metal atomic network during rapid heating and  
202 gradual cooling processes, known as *annealing* see Barca et al. (2015). During annealing, atoms  
203 within the metal reconfigure to a state of minimal energy maintenance cost. In this analogy, the  
204 arrangement of atoms corresponds to the configuration of sampling points, while the Objective  
205 Function (OF) mirrors the energy state of the system (Pardo-Igúzquiza 1998; Deutsch and Cockerham  
206 1994). Figure 2 illustrates the flowchart of SSA's operation, which can be understood as comprising  
207 a pre-processing stage followed by two nested loops. In the pre-processing phase, essential parameters  
208 required to start the optimization method are estimated, including the initial configuration ( $S_0$ ) and  
209 the initial temperature ( $T_0$ ).

210 The outer loop, reminiscent of temperature control in the physical analogy, stops as the temperature  
211 variable approaches zero. Conversely, the inner loop, linked to problem size ( $k$ ), iterates  $k$  times for  
212 a given temperature value. Within this inner loop, candidate solutions are generated and subjected to  
213 a decision rule. Consequently, the maximum number of iterations of the method is  $k \cdot N_{Temp}$ , where  
214  $N_{Temp}$  represents the total different temperature values assumed during the run. It is worth noting  
215 that the total number of iterations corresponds to the total number of processed network  
216 configurations. SSA evaluates a neighbouring configuration  $S_i$  of the current optimal configuration

217  $S^*$  at each step  $i$ , probabilistically deciding whether to move to  $S_i$  or remain in  $S^*$ . The transition  
 218 probability  $PT$  from the current configuration  $S^*$  to the candidate new configuration  $S_i$  is determined  
 219 by an acceptance probability function  $PT(S^* \rightarrow S_i)$ , which involves the OF values and temperature  
 220 ( $T$ ). The decision rule allows SSA to avoid being trapped in local optima by occasionally accepting  
 221 worse configurations. Typically, the neighbourhood search results in minimal changes to the current  
 222 optimal configuration, wherein only one randomly chosen monitoring location  $s_i^*$  within its  
 223 neighbourhood is altered. The initial configuration  $S_0$  is typically randomized by removing  $k$   
 224 locations from the original sampling scheme.  
 225



226 Fig. 2. The SSA working flowchart (adapted from Lobato et al. 2012)

227 Alternatively, a smart initialization, involving the application of a Greedy heuristic (Drosou and  
 228 Pitoura 2009) before starting SSA, can be applied. This heuristic provides a sub-optimal configuration  
 229 quickly, which can be used as  $S_0$  by SSA. The computational load increase due to the application of  
 230 the Greedy heuristic is offset by the faster convergence of SSA. SSA continues to run until a specified

231 stop criterion is met such as maximum iterations, persistence of the optimal transient solution, and  
 232 temperature threshold of the cooling scheme.

233

### 234 2.5. Variograms

235 Under the name of (semi)variogram, two different types of functions related to geographically  
 236 referenced data are usually denoted. The first type of function, the *experimental variogram*, is discrete  
 237 and represents the plot of the semivariance computed at different lags. The second type of function,  
 238 the *variogram model*, is parametric, continuous and conditionally negative definite (Castellini et al.,  
 239 2019). Model's parameters are the *nugget effect*, the *partial sill*,  $\sigma^2$  (that is the maximum variability  
 240 degree of the process net of noise) and the *range* ( $\alpha$ ) is the distance beyond which the spatial  
 241 correlation disappears. The Matérn model has a further parameter with respect the other models,  $k$ ,  
 242 called the *shape* while  $\mathcal{K}_k$  is the modified Bessel function of the second kind. All the reported  
 243 parameters are positive for definition. The models used in the present study are reported in the  
 244 following table in their analytical form.

245

246 *Table 1. Theoretical variograms reported in the present study.*

Model	Variogram	Parameter Restrictions
Spherical	$\gamma(h) = \sigma^2[(1 - h/\alpha)^2 + (1 + h/2\alpha)]$	
Gaussian	$\gamma(h) = \sigma^2(1 - \exp(-h^2/\alpha^2))$	
Matérn	$\gamma(h) = \sigma^2[1 - (\alpha h)^k \mathcal{K}_k(\alpha h)]$	$k > 0$

247

### 248 2.6. Automated variogram modelling

249 In the sampling downsizing optimization, a key role is played by the variogram model. In this study,  
 250 the model selection was based on an optimization tool which lists the theoretical models that best fit

251 the experimental variogram according to an objective function which expresses the difference  
 252 between the experimental variogram and the candidate model.

253 Automated, omnidirectional variogram model fitting takes place according to the following steps:

254 1. Let  $D$  be 0.35 times the length of the diagonal of the box that spans the data, i.e.

$$D = 0.35\sqrt{dx^2 + dy^2} \quad (\text{eq. 1})$$

255 with  $dx$  the range of  $x$  coordinates and  $dy$  the range of  $y$  coordinates of the data points;

256 2. for  $p$  distance intervals with boundaries 0, 2, 4, 6, 9, 12, 15, 25, 35, 50, 65, 80, and 100% of  $D$ , the  
 257 classical omnidirectional sample semi-variogram values  $\gamma_{exp}(h_i)$  at each  $h_i$  are computed as the  
 258 average distance of all point pairs falling within the distance interval  $i$ -th;

259 3. if the number of point pairs for lag  $i$ ,  $N_i$ , in the  $i$ th lag interval is smaller than 5, two distance  
 260 intervals are merged, the sample variogram recomputed and  $p$  lowered by one;

261 4. for the variogram model parameters as initial values the following are considered for the fit:

- 262 • sill: mean of the maximum and median value of the  $\gamma_{exp}(h_i)$ ;
- 263 • nugget: minimum value of the  $\gamma_{exp}(h_i)$ ;
- 264 • range:  $D/3.5$ , which is 10% of the length of the diagonal of the rectangle enveloping the data;
- 265 • a list of candidate values for the smoothness parameter  $k$  of the Matérn variogram model is  
 266 provided. For each variogram model type contained in a predefined list, the candidate  
 267 variogram model is tuned using a Gauss–Newton algorithm by minimising the weighted error  
 268 sum of squares

$$SSerr = \sum_{i=1}^N \frac{N_i}{h_i^2} \left( \gamma_{exp}(h_i) - \gamma_{theor}(h_i) \right)^2 \quad (\text{eq. 2})$$

269 with  $\gamma_{theor}(h_i)$  the variogram model value for distance  $h_i$ ;

270 5. Finally, the model (model type, nugget, sill, range,  $k$  in case of the Matérn model) with the smallest  
 271  $SSerr$  is selected.

272 These heuristic steps have been presented earlier in Hiemstra et al. (2009) and some of them in  
273 Pebesma (2004, 2005) and Pebesma and Wesseling (1998). In the present work, the model selection  
274 is based on a facility available in the R environment (library automap, function autofitvariogram).

275

### 276 *2.7. Sampling scheme optimization process*

277 A function of the Average Kriging Variance (AKV) was considered as objective function of the  
278 sampling scheme optimization process. Kriging estimation variance is a value provided by the kriging  
279 system in association to the predicted value and represents the uncertainty attached to the prediction.  
280 The adopted objective function follows the lines provided by Delhomme (1978) who described a  
281 suitable function for assessing an optimal reduced configuration on the basis of the areal average  
282 uncertainty. The relative change of the average kriging variance estimation is defined as:

$$\hat{\phi}_{AKV} = \frac{AKV_{Init} - AKV_i}{AKV_{Init}} \quad (\text{eq. 3})$$

283 where  $AKV_i$  is the average kriging variance assessed on a previously defined estimation grid and  
284 associated to the  $i$ -th reduced configuration and  $AKV_{Init}$  is the corresponding variance associated to  
285 the original complete sampling scheme. The relative change of average kriging variance can be  
286 interpreted as the quantity of information lost due to the scheme reduction.

287 A useful indicator to quantify the degradation degree of the information downstream the reduction  
288 process, i.e. the deviation from the full sampling design, is the *efficiency index*,

$$Efficiency\ Index = \frac{AKV_{Init}}{AKV_i} \quad (\text{eq. 4})$$

289 which is a value lesser than 1 because we expect that after a reduction the AKV will grow.

290 In this study, we evaluated a progressive reduction in the sampling points starting from a number of  
291 10 to 20 observations. Moreover, in order to assess the effect of information loss due to the sampling  
292 scheme reduction, theoretical variograms derived from the reduced sets of observations were  
293 computed and the goodness of fitting evaluated and analysed.

294        2.8. *Validation process*

295    After the reduction of the sampling scheme, a check is due to control the actual redundancy of the  
296    excluded points by predicting them from the reduced scheme (Barca et al., 2016). For this aim, a set  
297    of error metrics are computed, which provides the means to analyse the impact of the reduction.  
298    Generally, it is difficult to assign a qualitative degree (excellent, good or poor) to the goodness of fit  
299    since error indices generally lack a superior limit, this problem can be overcome by means of Equation  
300    5:

$$\text{MAPE}\% = \frac{1}{n} \sum_{i=1}^n \frac{|z^*(x_i) - z(x_i)|}{z(x_i)} = \frac{1}{n} \sum_{i=1}^n \frac{|r_i|}{z(x_i)} = \frac{1}{n} \sum_{i=1}^n \frac{r_i^a}{z(x_i)} * 100 \quad (\text{eq. 5})$$

301    The Mean absolute percentage error (MAPE) index is dimensionless since any residual is rescaled in  
302    terms of the corresponding observed value. Since it is an average relative value, it is possible to define  
303    thresholds of goodness of fit; for example, if MAPE is less than 0.1 (or 10% if it is expressed as a  
304    percentage), this can be considered a good result according to the Lewis scale (Lawrence and  
305    Klimberg, 2016; Barca et al., 2017). The R library used for using the error metrics mentioned above  
306    was {Metrics}.

307    The results of the validation allow also judging the kind of variogram model better suited to drive the  
308    reduction process. Moreover, the regression-kriging was applied (Barca et al., 2019) as it enables  
309    exploiting the ancillary information, and thus further improves the prediction of the excluded points.  
310    In this way, the effectiveness of the secondary information provided by proximal sensing could be  
311    exploited.

312

313        2.9. *Lin's agreement (concordance) coefficient*

314    To assess the strength of the concordance between two series of data, the Lin's agreement coefficient  
315    has been applied. Lin's agreement coefficient provides a measure of overall accuracy which takes  
316    into account both bias correction and precision. Bias correction is calculated from two bias measures:  
317    constant bias (location-shift) and systematic bias (scale-shift) (Barnhart et al., 2002). The precision

318 is provided by the Pearson's (r) correlation coefficient. The formula is the following (Stevenson et  
 319 al., 2018):

$$\rho_c = \frac{2 \cdot r \cdot \sigma_X \cdot \sigma_Y}{\sigma_Y^2 + \sigma_X^2 + (\mu_Y - \mu_X)^2} \quad (\text{eq. 6})$$

### 320 **3. Results**

#### 321 *3.1. Soil Organic Carbon map*

322 Descriptive statistics for the primary variable, SOC, considering the complete dataset (71 points) are  
 323 reported in Table 2. Basic statistics showed that the assumption of a normal distribution for the SOC  
 324 data was reasonable as confirmed by skewness and kurtosis values and by Shapiro-Wilk test (p =  
 325 0.678). For this reason, data were not subjected to a normal transform.

326

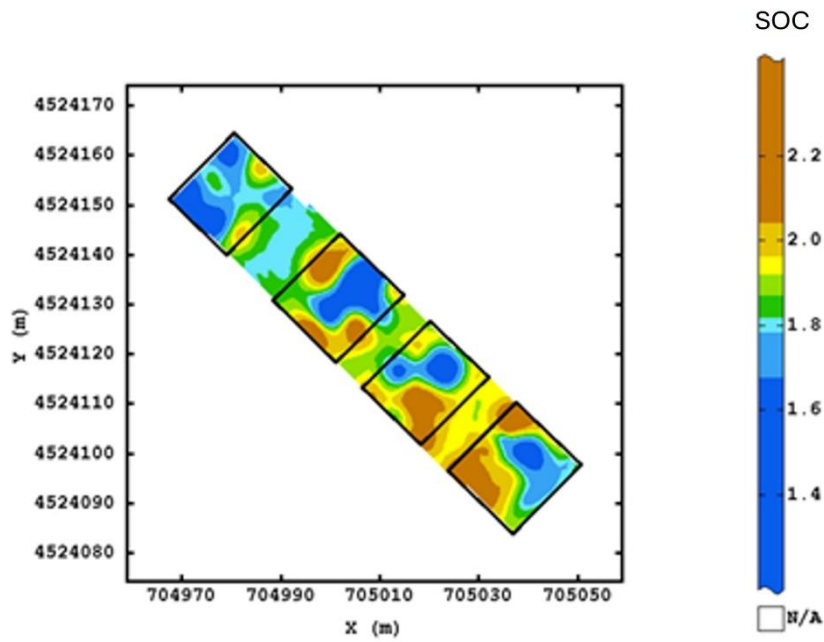
327 *Table 2. Summary statistics for SOC (g 100 g<sup>-1</sup>)*

<b>Variable</b>	<b>N</b>	<b>Mean</b>	<b>Sd</b>	<b>Min</b>	<b>Max</b>	<b>Skewness</b>	<b>Kurtosis</b>
<b>SOC</b>	71	1.85	0.28	1.19	2.43	-0.21	-0.29

328

329 A spherical model with a range of 7 m was fitted to the experimental variogram of SOC. The results  
 330 of the cross-validation test were satisfactory because Mean Error was quite close to 0 (ME = -0.00626)  
 331 and the Mean Square Standardized Error was 0.85. The MSSE was out of the tolerance interval (0.91  
 332 - 1.08) probably due to the smoothing of the modelling (Carroll and Cressie, 1996; Chilès and  
 333 Delfiner, 1999).

334 The spatial distribution of SOC estimated by ordinary kriging (OK) showed larger average values in  
 335 the southern part of the field (Fig. 3). The coarse sampling scale likely determined the high degree of  
 336 smoothness.



337

338 *Fig. 3. Spatial estimates of SOC (g 100 g<sup>-1</sup>). The black polygons indicate the four blocks in the RCB*  
 339 *experimental design.*

340

341 *3.2. Comparison of the impact of different theoretical variogram models to assess spatial*  
 342 *dependence of SOC values in the reduction of a previously defined sampling design*

343 In order to compare the effect of the variogram model on the sampling scheme reduction, different  
 344 theoretical models were compared. The variogram model optimization criterion (SS<sub>ERR</sub>; eq. 2) found,  
 345 for the SOC variable, Matérn and spherical as the best theoretical models for the complete dataset.

346 Both models showed good adaptation to the experimental variogram, with a slightly lower SS<sub>ERR</sub> for  
 347 the Matérn model (0.00304 vs 0.00307). In accordance, slightly higher values of Lin's correlation  
 348 concordance coefficients (eq. 6) and overall accuracy were observed for the Matérn model (0.59 and  
 349 0.91 vs 0.59 and 0.90, for Matérn and spherical models respectively).

350 Nugget variance for the nested spherical model fitted was zero. The two theoretical models found  
 351 close sill variance (approximately 0.08) as shown in Table 3.

352 *Table 3. Parameters of the two theoretical nested models fitted to the experimental variogram of*  
 353 *SOC complete dataset.*

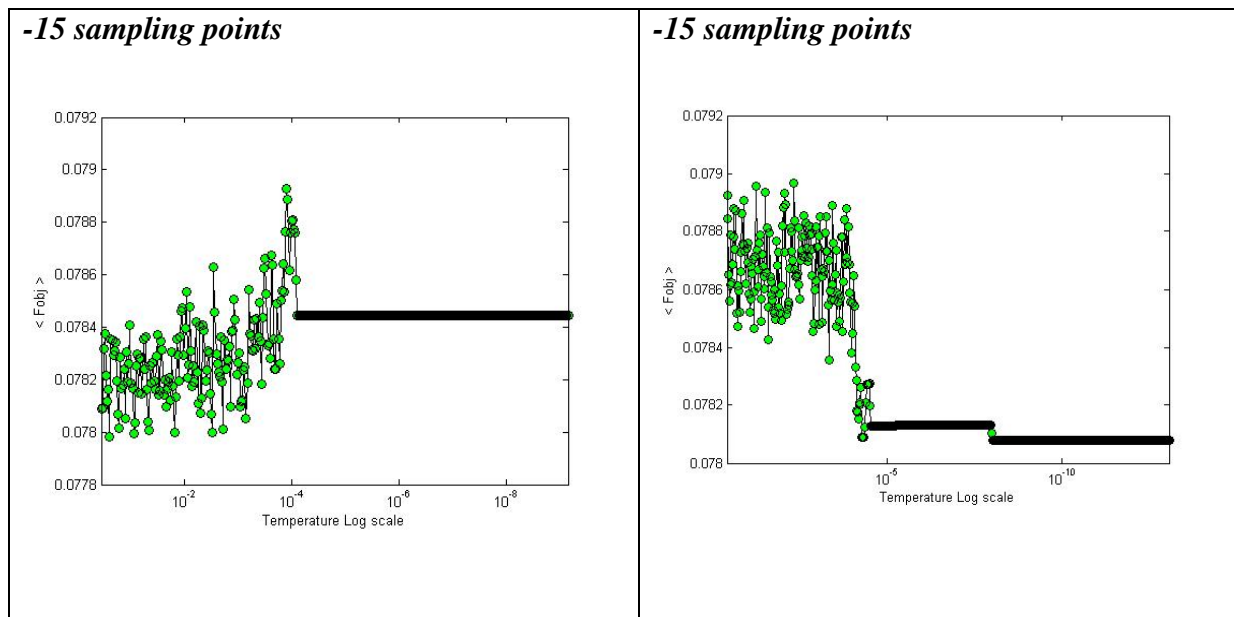
	<b>Nested model</b>	<b>Partial sill</b>	<b>Range</b>	<b>Shape (k)</b>
1	Nugget	0.01	0.0	
	Matérn	0.07	4.0	10
2	Spherical	0.08	7.7	

354

355 To initialize the iterative downsizing optimization process the parameters of the variogram model are  
 356 needed as an input.

357 The process was set up with a starting number of points to be dropped from the complete dataset (71  
 358 points) equal to 10, 15 and 20. The convergence graphs plot the values of the objective function  
 359 (average kriging variance, eq. 3) against the (log) temperature value assumed at each run. Inspecting  
 360 the convergence graphs within-models and between-models, it was possible to ascertain an average  
 361 behaviour of the convergence scheme for the two different models. Matérn model tended to get in  
 362 stuck to a suboptimal solution; in fact, better solutions were found at the initial steps of the process,  
 363 apart for the -20 downsizing stage. On the contrary, the spherical model appeared to aid the  
 364 convergence, showing to find always the global optimum. In Figure 4 the convergence graphs related  
 365 to the -15 downsizing stage are reported.

366



367 Fig. 4. Convergence graphs related to the two different variogram models, Matérn (left side) and  
 368 spherical (right side), in the -15 sampling points downsizing process performed considering the  
 369 primary variable (SOC).

370 These results were confirmed by the values assumed by the efficiency indices (EI, eq. 4), which were  
 371 slightly better for the spherical models and with an increasing deviation between the models at each  
 372 run (Table 4). Therefore, the reduced schemes appeared to have a similar and narrow information  
 373 loss.

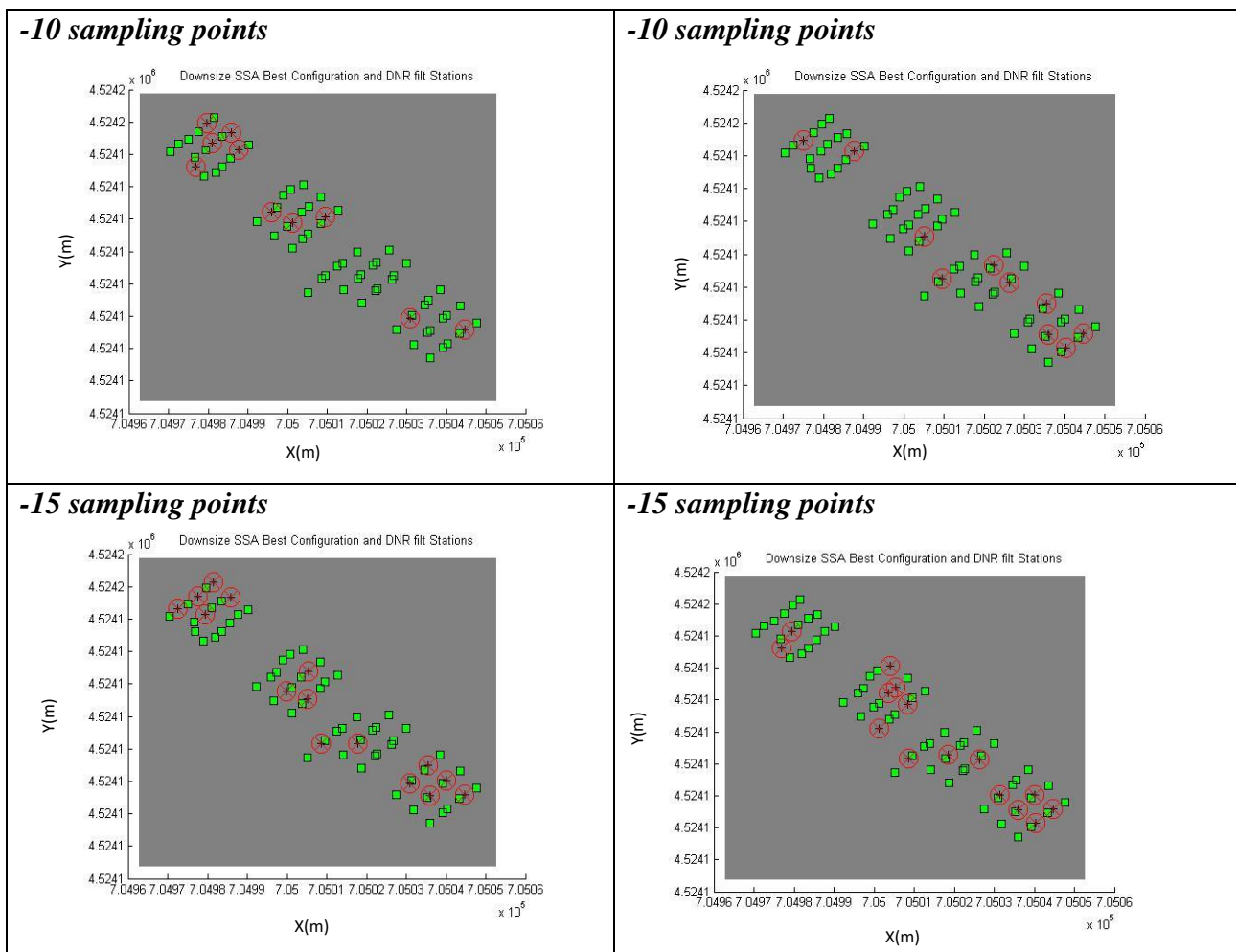
374 Table 4. Values of the efficiency index (EI) at convergence.

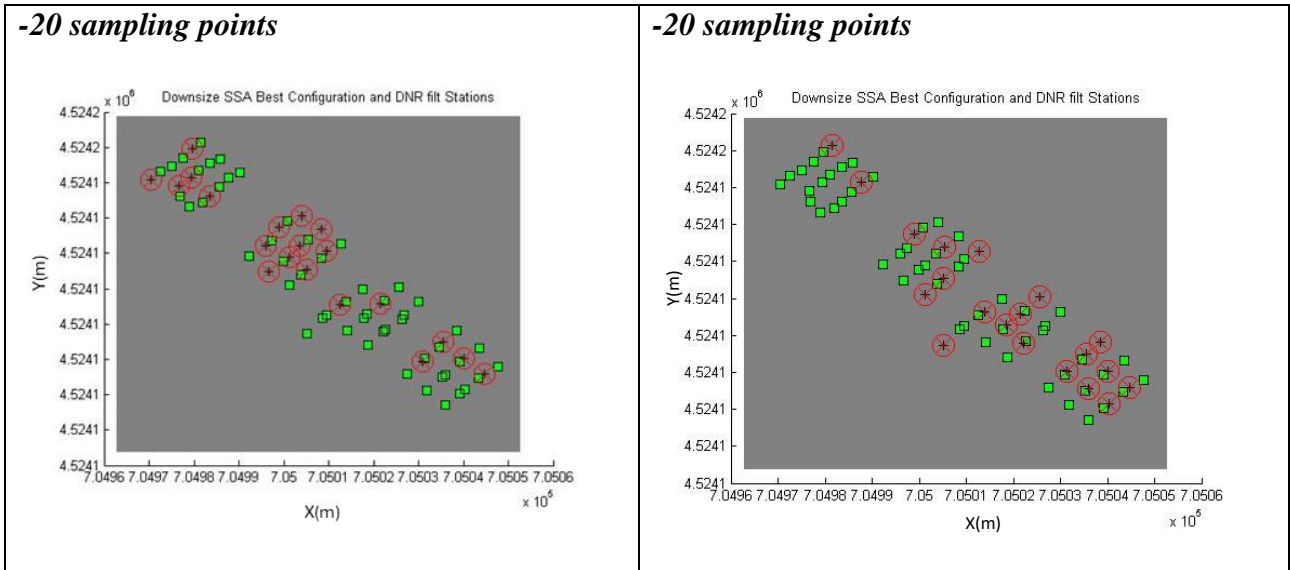
Nested models	Downsizing processes (EI)		
	-10	-15	-20
1 Nugget+Matérn	0.992	0.988	0.981
2 Spherical	0.996	0.991	0.988

375  
 376 In Figure 5 the optimized (reduced) sampling schemes, for the two theoretical models and to the  
 377 increase of dropped sampling points, are reported; by comparing the two dropped sets of points there  
 378 can be found low similarity between the schemes.

379 Therefore, the downsize following the two different variogram models resulted in two quite different  
380 optimized schemes, highlighting the role of the theoretical model applied in ruling the sampling  
381 reduction. Comparing the figures emerges major tendency of spherical variogram to almost equally  
382 distribute the dropped points over the different blocks with respect to the Matèrn variogram. The  
383 reduced sampling schemes showed in Figure 5 are gained without using the information contained in  
384 the GPR covariates but only SOC observations.

385





386 *Fig. 5. Optimal sampling configuration schemes obtained with the Matérn (left side) and spherical*  
 387 *(right side) models using only SOC observations.*

388 Table 5, where the number of sample points eliminated for each block is reported, clearly confirms  
 389 this result. An index of agreement to compare the different reduced configurations has been defined  
 390 as the cumulated absolute difference between the numbers of points dropped in each block (called  
 391 *delta (abs)*). These findings highlight that the selection of the appropriate variogram model is a critical  
 392 passage upstream the optimization process when a model-based optimization is pursued.

393

394

*Table 5. Comparison of the number of sampling points eliminated in each block in the reduced*

395

*sampling schemes obtained with the two theoretical models.*

	<b>Block I</b>	<b>Block II</b>	<b>Block III</b>	<b>Block IV</b>	Delta (abs)
Matérn (-10)	5	3	0	2	
Spherical (-10)	2	1	3	4	
deviations	3	2	3	2	10
Matérn (-15)	5	3	2	5	
Spherical (-15)	2	5	3	5	
deviations	3	2	1	0	6
Matérn (-20)	5	9	2	4	
Spherical (-20)	2	4	6	7	
deviations	3	5	4	3	15

396

397        *3.3. Assessment of the possibility of using covariate information, substituting the primary variable,*  
398                    *for the optimization process*

399        With the aim of assessing the possibility of using covariate information to support the optimization  
400        process for the primary variable, GPR data were considered.

401        The time slices for 600 MHz antenna were built within consecutive time windows of 2 to 10 ns, since  
402        the antenna showed a sensible attenuation of signal at about 10 ns (equal to about 0.50 m depth). GPR  
403        data at any time interval were correlated among them and this justified the multivariate approach. The  
404        data were previously transformed into standard Gaussian variables (since the hypothesis of normality  
405        was rejected) and a Linear Model of Co-regionalization was fitted to all experimental direct and cross-  
406        variograms with the following basic structures: Nugget effect and a Spherical model with a range of  
407        9m. Mean error was quite close to 0 and the mean square standardized error was almost 1.

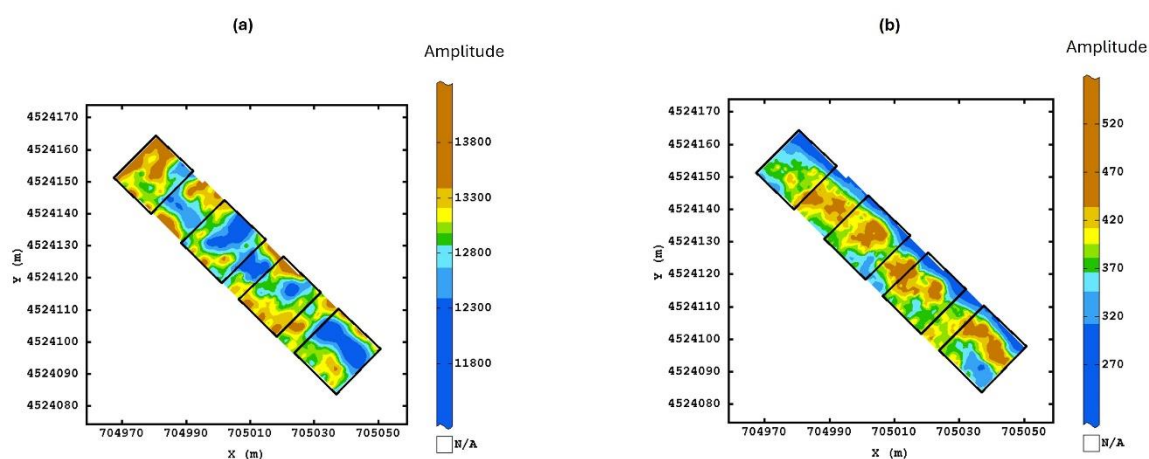
408        In Figure 6, only the results related to time slice at 2 ns (0.1 m depth) and 7 ns (0.35 m depth) were  
409        reported, because a discontinuity in the radar signal after 0.1m depth was observed and these  
410        time/depth maps were comparable with the depth of soil samples.

411        The amplitude map estimated at 0.10 m depth displayed lower values in the central part of the area.  
412        Starting from the 4ns time slice (0.2m-depth) until the 10ns time slice (0.50m-depth), the maps looked  
413        quite consistent with a wide central structure characterised by higher values. This may be indicative  
414        of some discontinuity along the vertical profile at 0.2m-depth.

415        The colour scale is always an iso-frequency scale to display the spatial structure, but the values of  
416        amplitude signal (in digital number) show the signal attenuation with the depth.

417

418



419 *Fig. 6. Time slices at 2ns and 7ns, corresponding to 0.1 m and 0.35 m depth, respectively (a and b).*

420 *Colour scale uses iso-frequency classes.*

421 From the visual inspection of the maps, apart the block in the northern area, a similar behaviour was  
 422 observed between the amplitude map estimated at 0.1 m depth and SOC spatial distribution (Fig. 3  
 423 and 6).

424 In order to identify the covariate variables most related to the primary variable (SOC), bivariate and  
 425 multivariate analysis approaches were used. To this aim, firstly the geostatistical estimates of the  
 426 selected geophysical variables were collocated into the point file by assessing, to each location and  
 427 for each variable, the nearest estimate. The relationships between SOC and GPR variables were first  
 428 explored through correlation analysis; afterwards a stepwise multiple linear regression analysis was  
 429 carried out to select the covariates most related to the primary soil property.

430 The analysis showed a highly significant relationship of SOC with amplitudes at 0.05m-depth, 0.1m-  
 431 depth and 0.5m-depth and a significant correlation with amplitudes at 0.15m-depth, 0.35m-depth and  
 432 0.4m-depth (Table 6).

433 Stepwise regression analysis results selected only amplitude at 0.1m-depth as significant variable for  
 434 explaining SOC variation ( $F=14.64$ ,  $P=0.0003$ ). For this reason, only this amplitude variable was  
 435 selected as proxy covariate for designing optimal scheme for SOC sampling.

436

Table 6. Correlation matrix between SOC complete dataset and GPR variables.

Pearson Correlation Coefficients, N=71, Prob &gt; |r| under H0: Rho=0

	SOC	ckAmp 0.05m	ckAmp 0.1m	ckAmp 0.15m	ckAmp 0.2m	ckAmp 0.25m	ckAmp 0.3m	ckAmp 0.35m	ckAmp 0.4m	ckAmp 0.45m	ckAmp 0.5m
<b>SOC</b>	1										
<b>ckAmp 0.05m</b>	0.314 0.007	1									
<b>ckAmp 0.1m</b>	0.418 0.0003	0.668 <.0001	1								
<b>ckAmp 0.15m</b>	0.279 0.018	-0.043 0.716	0.705 <.0001	1							
<b>ckAmp 0.2m</b>	0.189 0.114	-0.308 0.009	0.483 <.0001	0.95 <.0001	1						
<b>ckAmp 0.25m</b>	0.186 0.120	-0.354 0.002	0.424 0.0002	0.928 <.0001	0.990 <.0001	1					
<b>ckAmp 0.3m</b>	0.079 0.507	-0.571 <.0001	0.144 0.2285	0.746 <.0001	0.876 <.0001	0.923 <.0001	1				
<b>ckAmp 0.35m</b>	-0.300 0.010	-0.891 <.0001	-0.544 <.0001	0.098 0.4126	0.334 0.0044	0.379 0.0011	0.607 <.0001	1			
<b>ckAmp 0.4m</b>	-0.236 0.046	-0.687 <.0001	-0.426 0.0002	0.084 0.482	0.260 0.028	0.251 0.034	0.318 0.006	0.791 <.0001	1		
<b>ckAmp 0.45m</b>	-0.125 0.2956	-0.829 <.0001	-0.289 0.0143	0.412 0.0004	0.614 <.0001	0.626 <.0001	0.707 <.0001	0.827 <.0001	0.830 <.0001	1	
<b>ckAmp 0.5m</b>	-0.308 0.008	-0.936 <.0001	-0.550 <.0001	0.152 0.203	0.395 0.0007	0.423 0.0002	0.587 <.0001	0.898 <.0001	0.780 <.0001	0.918 <.0001	1

438 In grey shadow, the correlations of the GPR variables with SOC are highlighted.

440 The variogram model optimization criterion ( $SS_{ERR}$ ) found, for the GPR variable, the Gaussian and  
441 the spherical as the best theoretical models.

442 Both models showed good adaptation to the experimental variogram, with a slightly better  $SS_{ERR}$  for  
443 the Gaussian model ( $3.38 \times 10^{10}$  vs  $4.92 \times 10^{10}$ ). In accordance, slightly higher values of Lin's  
444 correlation concordance coefficients and overall accuracy were observed for the Gaussian model  
445 ( $0.87$  and  $0.99$  vs  $0.83$  and  $0.96$ , for Gaussian and spherical models respectively).

446 The parameters of the two theoretical nested models are reported in Table 7 and were used to optimize  
447 the sampling design. Nugget variance was null for both nested models fitted.

448

449 *Table 7. Parameters of the two theoretical nested models fitted to the experimental variogram of*  
450 *GPR data.*

	<b>Nested model</b>	<b>Partial sill</b>	<b>Range</b>
1	Gaussian	257413.4	4.73
2	Spherical	249483.2	10.28

451

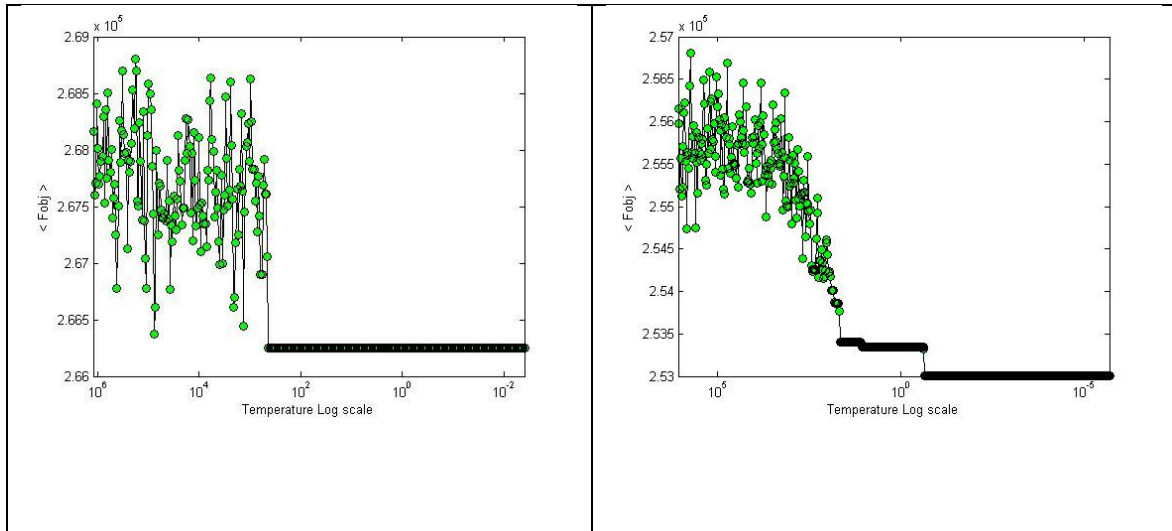
452 As for SOC sampling points' optimization, an iterative downsizing optimization process was set up  
453 with a starting number of points to be dropped equal to 10.

454 The downsize following the two different variogram models resulted in two quite different optimized  
455 schemes. Gaussian model, as observed also for Matérn model with the primary variable, seems to  
456 reach suboptimal solutions in comparison to the spherical model. The different behaviour is  
457 underlined by the baseline of the ordinate axis, which was always lower for the spherical model. The  
458 convergence graphs related to the -15 downsizing stage are reported as an example in the Figure 7.

459

460

<i>-15 sampling points</i>	<i>-15 sampling points</i>
----------------------------	----------------------------



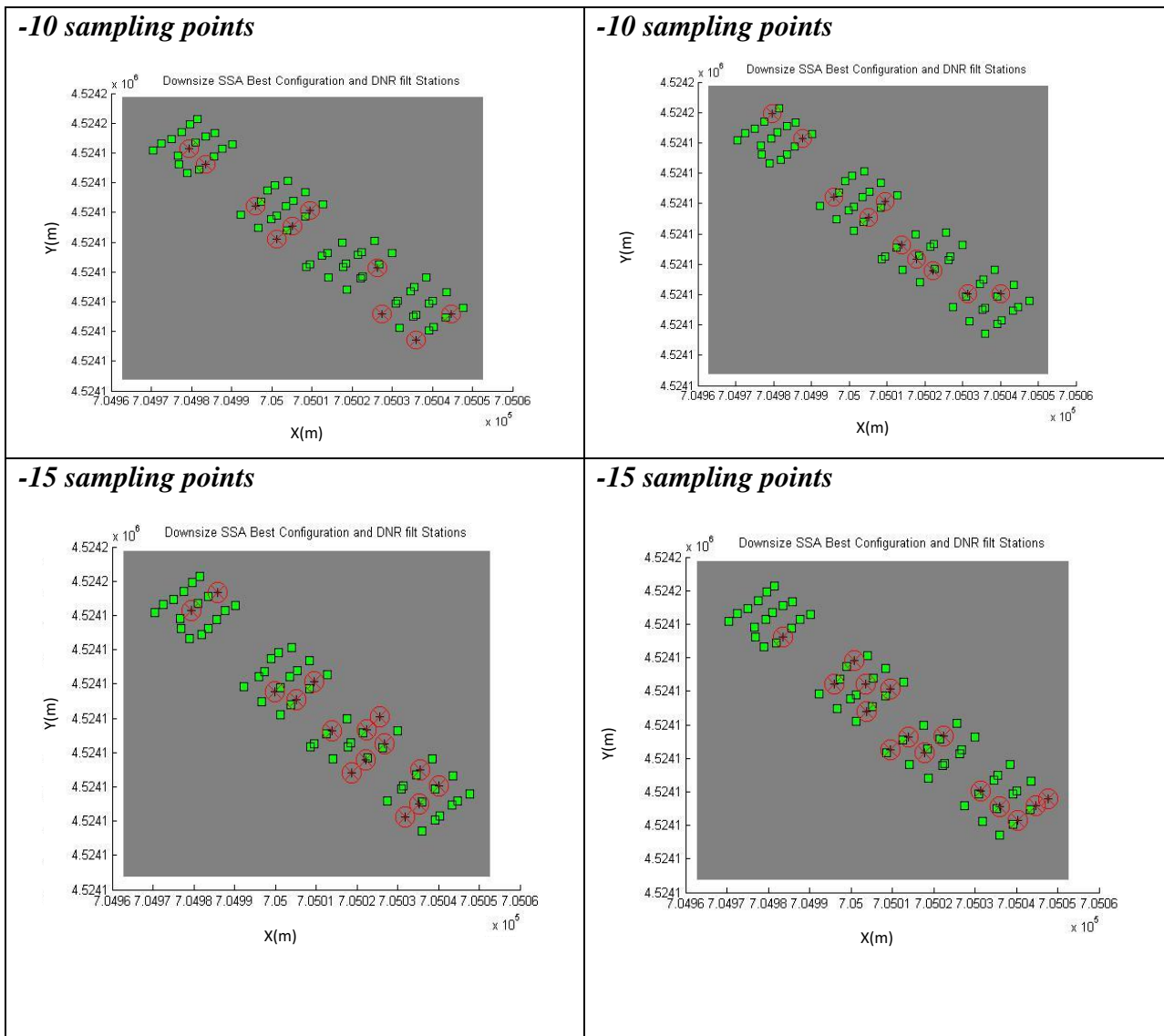
461 *Fig. 7. Convergence graphs related to the two different variogram models, Gaussian (left side) and*  
 462 *spherical (right side), in the -15 sampling points downsizing process, performed considering the*  
 463 *covariate GPR variable.*

464 The lower efficiency observed with the Gaussian variogram model is not completely confirmed by  
 465 the values assumed by the efficiency indices, reported in Table 8, which show always slightly better  
 466 values for the Gaussian in comparison to the spherical model.

467 *Table 8. Values of the efficiency index at convergence.*

Nested models	Downsizing processes (EI)		
	-10	-15	-20
1Gaussian	0.997	0.992	0.989
2Spherical	0.993	0.987	0.980

468  
 469 In Figure 8 the reduced sampling schemes, for the Gaussian and spherical models to the increase of  
 470 dropped sampling points, are reported; by comparing the two dropped sets of points there can be  
 471 found a sufficient agreement between the schemes particularly with a lower number of points  
 472 eliminated. Table 9, where the number of sample points eliminated in each block is reported, confirms  
 473 this result, with only 4 and 6 deviations when 10 and 15 points were dropped, respectively, as shown  
 474 by the delta (abs) index of agreement.



476 *Fig.8. Optimal sampling configuration schemes obtained with the Gaussian (left side) and spherical*  
 477 *(right side) models using the covariate GPR variable.*

478

479

480 *Table 9. Comparison of the number of sampling points eliminated in each block in the reduced*  
 481 *sampling schemes obtained with the two theoretical models using the covariate GPR variable.*

	Block I	Block II	Block III	Block IV	Delta (abs)
Gaussian (-10)	2	4	1	3	

Spherical (-10)	2	3	3	2	
deviations	0	1	2	1	4
Gaussian (-15)	2	3	6	4	
Spherical (-15)	1	5	4	5	
deviations	1	2	2	1	6
Gaussian (-20)	9	4	2	5	
Spherical (-20)	5	5	6	4	
deviations	4	1	4	1	10

482

483 Also, for the covariate, these findings highlight the critical role of the selection of the appropriate  
484 variogram model upstream the optimization process, when a model-based optimization is pursued.  
485 Comparing the reduced configurations garnered with the same variogram models but starting from  
486 the information provided by the primary (SOC) and the covariate (GPR) variables, it emerged a more  
487 similar behaviour with the use of the spherical model (Table 10) rather than that observed with the  
488 Matérn-Gaussian models (Table 11).

489 In particular, the first two configurations ( -10 and -15 points), obtained with the spherical model,  
490 resulted very close each other indicating that the covariate variable can play an important role in  
491 substituting the primary variable and opening interesting perspectives for further development in this  
492 research field. The Gaussian-Matérn models, notwithstanding the good results obtained at the  
493 optimization stage, underlined by the efficiency indices values, showed different optimized  
494 configurations, confirming once more the impact of the variogram model adopted in the sampling  
495 scheme optimization.

496

497 *Table 10. Number of sampling points eliminated in each block in the reduced sampling schemes.*

498 *Comparison between SOC e GPR reduction schemes obtained with the Spherical model..*

	Block I	Block II	Block III	Block IV	Delta (abs)
--	---------	----------	-----------	----------	-------------

Spherical SOC (-10)	2	1	3	4	
Spherical GPR (-10)	2	3	3	2	
deviations	0	2	0	2	4
Spherical SOC (-15)	2	5	3	5	
Spherical GPR (-15)	1	5	4	5	
deviations	1	0	1	0	2
Spherical SOC (-20)	2	4	6	7	
Spherical GPR (-20)	5	5	6	4	
deviations	3	1	0	3	7

499

500 *Table 11. Number of sampling points eliminated in each block in the reduced sampling schemes*  
501 *obtained with the Gaussian/Matérn models with the primary, SOC, and the covariate, GPR,*  
502 *variable.*

	<b>Block I</b>	<b>Block II</b>	<b>Block III</b>	<b>Block IV</b>	Delta (abs)
Matérn SOC (-10)	5	3	0	2	
Gaussian GPR (-10)	2	4	1	3	
deviations	3	1	1	1	6
Matérn SOC (-15)	5	3	2	5	
Gaussian GPR (-15)	2	3	6	4	
deviations	3	0	4	1	8
Matérn SOC (-20)	5	9	2	4	
Gaussian GPR (-20)	9	4	2	5	
deviations	4	5	0	1	10

503

504 Finally, to assess the impact of sampling scheme reduction, theoretical variograms were fitted on the  
505 reduced sets of points using the same models selected in the previous data analysis step.

506 By comparing the theoretical nested models fitted to the experimental variogram of SOC data with a  
507 progressively reduced sampling points number (full dataset, -10, -15, -20 sampling points), as a

508 general behaviour, a constant decrease of the concordance indices was observed for both the  
509 considered models (Table 12). In details, an average decrease from 0.59 to 0.14 was recorded for the  
510 Lin's concordance coefficient for the two theoretical models. In addition, although starting from very  
511 close initial values (full dataset, 0.59 and 0.5847 for the Matérn and spherical model, respectively),  
512 to the reduction of sampling point number, the Matérn model showed a better performance with  
513 values always larger than those observed for the spherical model (Table 12). Matérn model showed  
514 thus to be more resilient to modifications of the operative conditions. The results show that, under  
515 our experimental conditions, the downsizing can be considered acceptable up to a discard of 15  
516 sampling points (about 20% less), which caused a decrement of the Lin's CCC of about 24%. A  
517 further downsizing of other 5 sampling points caused a severe fall of the goodness of fitting, with a  
518 dramatic reduction of Lin's CCC of about 78%, in comparison to the full dataset.

519

520 *Table 12. Parameters of the two theoretical nested models (Spherical, on the left side, and Matérn*  
 521 *models, on the right side) fitted to the experimental variogram of SOC data with a progressively*  
 522 *reduced sampling points number (full dataset, -10, -15, -20 sampling points).*

Full dataset				Full dataset				
	Nested model	partial sill	range		Nested model	partial sill	range	shape
1	Nugget	0.0	0.0	1	Nugget	0.0108	0.0	
2	Spherical	0.080	7.673	2	Matérn	0.071	3.986	10
	Overall CCC	0.584			Overall CCC	0.590		
	Overall precision	0.653			Overall precision	0.650		
	Overall accuracy	0.894			Overall accuracy	0.907		
- 10 sampling points				- 10 sampling points				
	Nested model	partial sill	range		Nested model	partial sill	range	shape
1	Nugget	0.010	0.0	1	Nugget	0.018	0.0	
2	Spherical	0.075	6.951	2	Matérn	0.071	4.046	5
	Overall CCC	0.457			Overall CCC	0.504		
	Overall precision	0.588			Overall precision	0.603		
	Overall accuracy	0.777			Overall accuracy	0.835		
- 15 sampling points				- 15 sampling points				
	Nested model	partial sill	range		Nested model	partial sill	range	shape
1	Nugget	0.0	0.0	1	Nugget	0.007	0.0	
2	Spherical	0.053	8.506	2	Matérn	0.062	4.332	10
	Overall CCC	0.418			Overall CCC	0.447		
	Overall precision	0.521			Overall precision	0.545		
	Overall accuracy	0.802			Overall accuracy	0.821		
- 20 sampling points				- 20 sampling points				
	Nested model	partial sill	range		Nested model	partial sill	range	shape
1	Nugget	0	0	1	Nugget	0	0	0
2	Spherical	0.068	8.129	2	Matérn	0.069	3.577	10
	Overall CCC	0.127			Overall CCC	0.148		
	Overall precision	0.163			Overall precision	0.180		
	Overall accuracy	0.780			Overall accuracy	0.820		

523

524 By comparing the theoretical nested models fitted to the experimental variogram of GPR data, a  
525 similar general behaviour was observed (Table 13). In details, a decrease from an average value of  
526 0.84 to 0.60 was recorded for the Lin's concordance coefficient. Even in this case, although starting  
527 from very close initial values (full dataset, 0.87 and 0.83 for the Gaussian and spherical model,  
528 respectively), to the reduction of sampling point number, the Gaussian model showed a better  
529 performance with values of the coefficients always larger than those observed for the spherical model  
530 (Table 13). Gaussian model, similarly to the Matérn model, showed thus to be more resilient to  
531 modifications of the operative conditions with respect to the spherical model. The downsizing showed  
532 optimal conditions up to a discard of 15 sampling points, with an average decrement of the Lin's CCC  
533 of about 14%. A further downsizing caused a decrease of the goodness of fitting, with a reduction of  
534 Lin's CCC of about 28%, in comparison to the full dataset. The last reduction impacted more severely  
535 on the spherical model, where a decrement of about 36% was recorded.

536

537 *Table 13. Parameters of the two theoretical nested models (Spherical, on the left side, and Matérn*  
538 *models, on the right side) fitted to the experimental variogram of GPR data with a progressively*  
539 *reduced sampling points number (full dataset, -10, -15, -20 sampling points).*

<b>Full dataset</b>			<b>Full dataset</b>		
<i>Nested model</i>	<i>partial sill</i>	<i>range</i>	<i>Nested model</i>	<i>partial sill</i>	<i>range</i>
1 Nugget	0.0	0.0	1 Nugget	0.0	0.0
2 Spherical	249483.2	10.276	2 Gaussian	257413.4	4.729
<i>Overall CCC</i>	0.829		<i>Overall CCC</i>	0.868	
<i>Overall precision</i>	0.865		<i>Overall precision</i>	0.875	
<i>Overall accuracy</i>	0.958		<i>Overall accuracy</i>	0.991	
<b>- 10 sampling points</b>			<b>- 10 sampling points</b>		
<i>Nested model</i>	<i>partial sill</i>	<i>range</i>	<i>Nested model</i>	<i>partial sill</i>	<i>range</i>
1 Nugget	0.0	0.0	1 Nugget	0.0	0.0
2 Spherical	272137.4	10.681	2 Gaussian	294255.2	4.823
<i>Overall CCC</i>	0.780		<i>Overall CCC</i>	0.858	
<i>Overall precision</i>	0.820		<i>Overall precision</i>	0.870	
<i>Overall accuracy</i>	0.951		<i>Overall accuracy</i>	0.986	
<b>- 15 sampling points</b>			<b>- 15 sampling points</b>		
<i>Nested model</i>	<i>partial sill</i>	<i>range</i>	<i>Nested model</i>	<i>partial sill</i>	<i>range</i>
1 Nugget	0.0	0.0	1 Nugget	0.0	0.0
2 Spherical	265827.9	11.574	2 Gaussian	251744.8	5.294
<i>Overall CCC</i>	0.703		<i>Overall CCC</i>	0.745	
<i>Overall precision</i>	0.746		<i>Overall precision</i>	0.762	
<i>Overall accuracy</i>	0.941		<i>Overall accuracy</i>	0.978	
<b>- 20 sampling points</b>			<b>- 20 sampling points</b>		
<i>Nested model</i>	<i>partial sill</i>	<i>range</i>	<i>Nested model</i>	<i>partial sill</i>	<i>range</i>
1 Nugget	0	0	1 Nugget	0	0
2 Spherical	231990.3	8.440	2 Gaussian	288129	4.794
<i>Overall CCC</i>	0.533		<i>Overall CCC</i>	0.668	
<i>Overall precision</i>	0.656		<i>Overall precision</i>	0.715	
<i>Overall accuracy</i>	0.812		<i>Overall accuracy</i>	0.934	

541 *3.4.Final validation*

542 As a conclusive test, the dropped 15 points, representing the optimal downsizing condition among  
 543 those examined, were predicted starting from the reduced sampling dataset by means of the two  
 544 different variogram models and the kriging predictor (ordinary kriging). The models used are those  
 545 showed in Table 12 and 13 associated to the reduced schemes. In Table 14, a set of error metrics,  
 546 related to the prediction of the dropped points for SOC values, is reported. Results can be considered  
 547 nearly optimal and substantially equivalent for both models.

548

549 *Table 14. Error indices of SOC dropped points estimation under different models.*

<b>Model</b>	<b>MBE</b>	<b>RMSE</b>	<b>MAE</b>	<b>MAPE%</b>	<b>MAX</b>	<b>MIN</b>
Matèrn	-0.02	0.24	0.20	11	0.35	-0.42
Spherical	0.09	0.24	0.18	11.8	0.54	-0.25

550

551 Table 15 reports error metrics related to the reduction of GPR point scheme. The garnered values  
 552 could be misleading as the variable has a large order of magnitude; therefore, to express a correct  
 553 judgement the focus should be put on MAPE% (eq. 5). Such index highlights the substantial  
 554 equivalence between the two models. MAPE% showed relative errors around 1% that can be  
 555 considered a negligible quantity.

556

557 *Table 15. Error indices of GPR dropped points estimation under different models.*

<b>Model</b>	<b>MBE</b>	<b>RMSE</b>	<b>MAE</b>	<b>MAPE%</b>	<b>MAX</b>	<b>MIN</b>
Gaussian	-76.84	234.32	156.84	1.2	232.69	-747.48
Spherical	11.1	180.38	140.86	1.1	478.49	-202.61

558 Finally, regression-kriging was applied to exploit the secondary information in predicting the points  
 559 dropped from SOC scheme. According to the metrics values reported in Table 16, the spherical model  
 560 seems more capable to take advantage from exploiting secondary information than Matèrn model. A

561 possible explanation can be that the points being dropped are better selected during downsize process  
 562 by the spherical model rather than by Matèrn one. Another more interesting explanation highlights  
 563 larger similarities between the reduced sets of primary and secondary variables, respectively, when  
 564 spherical model is considered as a driver of the reduction process (Table 10). On the contrary, the  
 565 reduced sets are quite different between primary and secondary variables if the driver is Matèrn model  
 566 (Table 11).

567 *Table 16. Error indices of SOC dropped points estimation under different models with regression-*  
 568 *kriging.*

<b>Model</b>	<b>MBE</b>	<b>RMSE</b>	<b>MAE</b>	<b>MAPE%</b>	<b>MAX</b>	<b>MIN</b>
Matèrn	-0.05	0.25	0.20	11	0.36	-0.53
Spherical	0.06	0.20	0.16	10.3	0.40	-0.32

569  
 570 In conclusion, it appears that the spherical model approximates slightly worse the experimental  
 571 variogram of the reduced sampling scheme but selects better the redundant points to be reduced,  
 572 whereas Matèrn seems to approximate better the experimental variogram after the sampling scheme  
 573 reduction but is less effective to select actually redundant points from the original sampling scheme.  
 574 These results open interesting perspectives to future studies.

575

#### 576 **4. Discussion**

577 Appropriate sampling strategy and data analysis play a crucial role in agronomic and environmental  
 578 field research to assess i) the variability that occurs at a scale smaller than the block size in traditional  
 579 experimental designs; ii) the spatial dependence of observations and residuals. This information is  
 580 invaluable to analyse the treatment significance.

581 This study was aimed at defining advances in sampling design optimization for a key soil variable,  
 582 SOC, investigating the effect of the choice of the variogram model and of the use of covariate

583 information when a downsizing of a sampling scheme was pursued. In addition, a strategy to assess  
584 the optimal downsizing, based on the variogram fitting, was defined.

585 Gaussian and Matérn models showed to be more resilient to modifications of the operative conditions  
586 with respect to the spherical model. The better performance of the Matérn and Gaussian models can  
587 be attributed to their greater flexibility with respect to the spherical model. These findings highlight  
588 the critical role of the selection of the appropriate variogram model upstream the optimization  
589 process, when a model-based optimization is pursued.

590 The results showed that, under our experimental conditions, the downsizing can be considered  
591 acceptable up to a discard of 15 sampling points (about 20% less), which caused a decrement of the  
592 Lin's CCC of about 24% for SOC. A further downsizing of other 5 sampling points caused a severe  
593 fall of the goodness of fitting, with a dramatic reduction of Lin's CCC of about 78%, in comparison  
594 to the full dataset.

595 Comparing the reduced configurations garnered with the same variogram models but starting from  
596 the information provided by the primary (SOC) and the covariate (GPR) variables, it emerged a more  
597 similar behaviour with the use of the spherical model rather than that observed with the Matérn-  
598 Gaussian models. The configurations (less 10 and 15 points) obtained with the spherical model  
599 resulted very close each other indicating that the covariate variable can play an important role in  
600 substituting the primary variable and opening interesting perspectives for further development in this  
601 research field. The Gaussian-Matérn models, notwithstanding the good results obtained at the  
602 optimization stage, underlined by the efficiency indices values, showed different optimized  
603 configurations, confirming once more the impact of the variogram model adopted in the optimization  
604 of the sampling scheme.

605 The methodology proposed was assessed within an agronomic field experiment. The issue of the  
606 optimization of the sampling design, by minimizing at the same time the information loss, is in fact  
607 particularly relevant in agronomic research, where the need to assess the spatial correlation of the  
608 investigated variables, both for improving data analysis methods and for spatial interpolation, requires

609 the collection of large datasets with georeferenced data. The size of the study area does not affect the  
610 methodology proposed whose applicability depends on the presence of a significant spatial  
611 correlation structure for the primary variable and on the availability of appropriate covariate variables.

612

## 613 **5. Conclusions**

614 The primary aim of this study was to optimally reduce an initially oversized sampling plan for  
615 assessing soil total organic carbon (SOC). Our analysis demonstrated that it was possible to reduce  
616 the original sampling scheme by approximately 20% — equivalent to eliminating 15 sampling points  
617 out of 71 — without compromising the predictive capability of the sampling scheme. As concerns  
618 the reduced configuration, the spherical variogram model proved to be the most effective in  
619 identifying and removing redundant sampling points. This reduction process preserved the integrity  
620 and precision of the SOC assessment. By maintaining robust predictive performance despite the  
621 reduction in sample size, we have shown that the optimized sampling plan effectively balances  
622 efficiency with informational accuracy.

623 The results of our investigation showed that the GPR covariate had an important role both in  
624 improving the optimization of the sampling scheme for SOC and in replacing the primary variable to  
625 optimize the sampling scheme. Therefore, the use of relatively easy, accurate, and inexpensive  
626 geophysical methods can represent a viable solution to obtain the information needed to advance the  
627 precision agriculture.

628

## 629 **Author Contributions**

630 Conceptualization, A.M.S., E.B. and D.D.B.; methodology, E.B.; software, E.B.; validation, E.B.,  
631 D.D.B., A.M.S.; formal analysis, E.B., A.M.S. and D.D.B.; investigation, D.D.B.; data curation,  
632 D.D.B.; writing—original draft preparation, E.B.; writing—review and editing, D.D.B., A.M.S.,  
633 E.B.; visualization, D.D.B.; supervision, A.M.S. and E.B.; project administration and funding  
634 acquisition, A.M.S. All authors have read and agreed to the published version of the manuscript.

635

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